

**Table S1. Chemical Reaction Scheme (with Parameters) for Stochastic Simulations of Two-State Tat Positive-Feedback Model, Related to Figure 3**

<i>Reactions</i>	<i>Description</i>	<i>Rate and Value</i>
$\text{LTR}_{\text{OFF}} \leftrightarrow \text{LTR}_{\text{ON}}$	Promoter toggling from active to inactive state (basal transcription rate)	$k_{\text{on}} = \text{varied}$ ; $k_{\text{off}} = 0.01$ (for Fig. 3B $k_{\text{on}} = 0.0001$ )
$\text{LTR}_{\text{ON}} \rightarrow \text{mRNA} + \text{LTR}_{\text{ON}}$	Transcription of mRNA encoding Tat	$k_{\text{m}} = 1$
$\text{mRNA} \rightarrow \text{mRNA} + \text{Tat}$	Translation	$k_{\text{p}} = 10$
$\text{Tat} + \text{LTR}_{\text{ON}} \leftrightarrow \text{LTR}_{\text{ON-Tat}}$	Tat binding/unbinding to LTR (TAR)	$k_{\text{bind}} = .01$ ; $k_{\text{unbind}} = .01$
$\text{LTR}_{\text{ON-Tat}} \rightarrow \text{LTR}_{\text{ON-Tat}} + \text{mRNA}$	Transactivated rate of transcription	$k_{\text{transact}} = 5$ (varied in Fig. S2J)
$\text{mRNA} \rightarrow \otimes$	mRNA decay	$\delta_{\text{m}} = 1$
$\text{Tat} \rightarrow \otimes$	Tat decay	$\delta_{\text{p}} = 0.125$ (based on 8-hr $t_{\text{avg}}$ )

\*Initial conditions for all species except  $\text{LTR}_{\text{ON}}$  were set to zero ( $\text{LTR}_{\text{ON}} = 1$  at  $t = 0$ )