A History and Applications of Network Analysis



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Outline



- Origins in Graph Theory
- Origins in Social Dynamic Analysis
- The Internet and Modern-day Network Science
- Some Current Applications of Network Analysis

Graph Theory



- Network Analysis is rooted in graph theory: "the mathematical theory of the properties and applications of graphs"
 - A graph is a mathematical object G = (V, E), where
 - V = vertex set
 - E = edge set describing relationships among vertices $u, v \in V$
- Subtlety here: network and graph are often used interchangeably
 - A network is the relational representation of a complex system
 - A graph is the mathematical object that we inevitably analyze

Graph Theory Beginnings: Leonard Euler



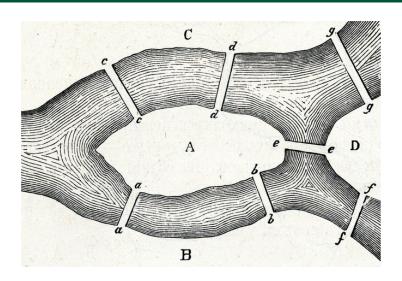


- Swiss mathematician and logician (1707 1783)
- Network analysis begins with solution to the "Bridges of Königsberg" question in 1735



The Seven Bridges of Königsberg





The Seven Bridges of Königsberg



- Big Question: Can one walk across all seven bridges and never cross the same one twice?
- Euler represented each of the four land areas separated by the river with letters A, B, C, and D
- Edges represented bridges between them
- Simple observation: if there is a path crossing all bridges, but never the same bridge twice, then nodes with odd number of links must be either the starting or the end point of this path

Ch. 2 of http://barabasi.com/networksciencebook/



Roots in Social Science: Jacob L. Moreno





- Austrian American psychiatrist (1889 1974)
- Key interest in the dynamics of social interactions within groups of people

The birth of social network analysis



- Moreno immigrated to New York in 1930
- March, 1933 gave a talk at a medical conference in New York
 City, discussing the first social network studies
- In 1934, he published a book on his studies Who Shall Survive, which contains the seeds of sociometry, now known as social network analysis
- Book depicted sociograms a new model for human interactions

The First Social Network: Sociograms



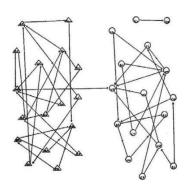


Figure: An early hand-drawn image of a social network, taken from *Who Shall Survive*, depicting friendship patterns between the boys (triangles) and girls (circles) in a class of schoolchildren in the 1930s.

In Contrast: Social Networks Today





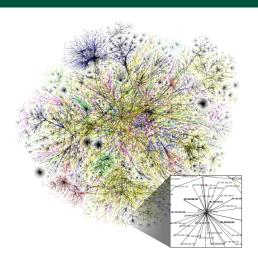
Interest in Social Networks



- Many possible definitions of an edge!
 - professional relationships
 - exchange of goods or money
 - communication
 - romantic or sexual relationships
- Can be used to understand a wide array of social dynamics
- Modern day look at online communities such as LinkedIn, Twitter, or Facebook, dynamics of animals, voting behavior of Senators, etc.

The Internet: Kickstarting modern-day Network Analysis





The Internet



- Vertices computers
- Edges physical connections between them, e.g., optical fiber cables or telephone lines
- Questions of Interest:
 - understanding centralized control
 - transferral of data
 - avoid bottlenecks and improve efficiency

Interestingly, we do not completely understand the structure of the internet and must rely on experiments for approximation

The World Wide Web



- Vertices web pages
- Edges hyperlinks between them
- Questions of Interest:
 - The "importance" of a webpage (HITS / PageRank)
 - Spread of ideas (cascades, information dissemination)
 - Spread of news

Network Neuroscience



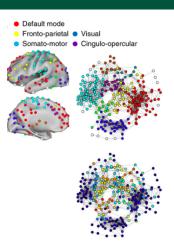


Figure: Networks in cognitive neuroscience.

Network Neuroscience



- Vertices regions of the brain
- Edges structural or functional interactions
- Questions of Interest:
 - Segmentation of functional and physical regions
 - Blood flow and effects on cognition
 - Differences between networks and disease

Biological Networks



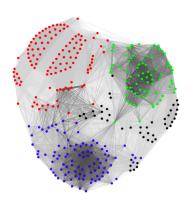


Figure: Network representation of relationships between *E-coli* strains among patients with urinary tract infection.

Biological Networks



- Vertices genes, chromosomes, SNPs
- Edges structural or functional interactions
- Questions of Interest:
 - Segmentation and relationship with clinical outcomes (cancer, antibiotic resistance, etc.)
 - Driver genes collections?
 - Causal relationship between vertices?
 - Differences among individuals

And the list goes on...



- Power grid networks
- Transportation (air, subway, road systems)
- Migration networks
- Textual networks
- Citation networks
- Recommendation networks

Bringing it all together



- Network science has a long history (1735!)
- Inherently interdisciplinary! (biology, physics, mathematics, sociologists, statisticians)
- Networks are "a way of thinking" and can provide a unique way to extract information from a system...
- ... now on to the good stuff