Course Topics

Measure Theory & Integration

- Measures
- Measurability
- Sigma Algebra
- Lebesgue Measure
- Lebesgue Integral
- Lebesgue's Dominated Convergence Theorem
- Monotone Convergence Theorem for Lebesgue
- Lebesgue Integrability
- Bochner's Sigma Algebra
- Properties of the Lebesgue Integral
- $L^p$ Spaces
- Hölder's & Fatou's Inequality
- Measurable Functions
- Simple Functions
- Comparisons of Riemann & Lebesgue Integrals
- Interchanging sums, limits, and integrals
- Sets of Measure Zero
- Inner & Outer Measure
- Measurable Spaces
- Lebesgue Integral's Completion of Riemann's
- Approximating Measurable Functions by Continuous Ones
- Lebesgue's Theorem
- Vitali-Carathéodory Convergence in Measure
- Lebesgue's Theorem
- Young's Inequality
- Hölder's Inequality
- Lebesgue Differentiation
- Product Measures
- Fundamental Theorem of Calculus for Lebesgue Integral